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CFA Level II

Equity Investments

Return Concepts I

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Contents

- ❖ Realized holding period return, expected HPR, required return, return from convergence of price to intrinsic value, discount rate, and internal rate of return.
- ❖ Equity risk premium based on historical and forward-looking models
- ❖ CAPM, Fama-French model, Pastor-Stambaugh model, macroeconomic multifactor models and the build-up method.





Learning Outcome Statement 31

LOS 31.a: distinguish among realized holding period return, expected holding period return, required return, return from convergence of price to intrinsic value, discount rate, and internal rate of return.

- ❑ Holding period return: the sum of current yield (or cash flow yield) and capital gain.

$$\text{holding period return } r = \frac{P_1 - P_0 + CF_1}{P_0} = \frac{P_1 - P_0}{P_0} + \frac{CF_1}{P_0}$$

- ❑ Annualized HPR is $(1 + r)^n - 1$



Learning Outcome Statement 31

LOS 31.a: distinguish among realized holding period return, expected holding period return, required return, return from convergence of price to intrinsic value, discount rate, and internal rate of return.

- ☐ Realized return – observed historical return.
- ☐ Expected return – based on forecasts of future prices and cash flows.
- ☐ Required return – the minimum return an investor requires given the asset's risk.
- ☐ Discount rate – the rate used to find the present value of an investment.



Learning Outcome Statement 31

LOS 31.a: distinguish among realized holding period return, expected holding period return, required return, return from convergence of price to intrinsic value, discount rate, and internal rate of return.

- ☐ Return from convergence of price to intrinsic value:

$$\frac{V_0 - P_0}{P_0}.$$

- ☐ Expected return is the sum of required return and return from convergence of price to intrinsic value.
- ☐ Internal rate of return – the rate that equates the value of the discounted cash flows to the current price of the security.



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

- ☐ Equity risk premium = required return on equity index – risk-free rate
- ☐ The risk-free rate should correspond to the time horizon for the investment
- ☐ Note that an equity risk premium is an estimated value and may not be realized.



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

- ❑ Historical estimate of equity risk premium
= historical mean return for equity market index
- risk-free rate
- Strength: simple and objective, unbiased if investors are rational
- Weakness: assume constant mean and variance of the returns over time; biased if only firms that have survived during the estimate period (called survivorship bias)



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

- ❑ Forward-looking (or ex ante estimates) use current information and expectations concerning economic and financial variables.
 - Strength: doesn't rely on stationarity assumption and less subject to survivorship bias.
- ❑ There are three main categories of forward-looking estimates: Gordon growth model, supply-side models and estimates from surveys.



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

- I. Gordon growth model (a.k.a constant growth model)
- Useful for developed economics and markets.
 - GGM equity risk premium=
(1-year forecasted dividend yield on market index)
+ (consensus long-term earnings growth rate)
- (long-term government bond yield)



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

I. Gordon growth model (a.k.a constant growth model).

E.g. suppose company A's dividend yield is 2%, growth expectation is 6%, and long-term bond yields is 6%. What is GGM equity risk premium?

Ansner: $(2+6-6)\%=2\%$

- Weakness: (1) the forward-looking estimates will change through time and need to be updated. (2) assume stable growth rate, not appropriate in rapidly growing economies.



Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

For fast-growing economics, use the following forward-looking model.

$$\text{Equity index price} = PV_{rapid}(r) + PV_{transition}(r) + PV_{mature}(r)$$





Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

II. Macroeconomic Models (Supply-side estimates).

- Based on the relationships between macroeconomic variables and financial variables
- Strength: use proven models and current information
- Weakness: only appropriate for developed countries





Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

II. Macroeconomic Models (Supply-side estimates).

□ Ibbotson-Chen (2003) model

$$\text{equity risk premium} = [1 + \hat{i}] \times [1 + \widehat{rEg}] \times [1 + \widehat{PEg}] - 1 + \hat{Y} - \widehat{RF}$$

where:

\hat{i} = expected inflation

\widehat{rEg} = expected real growth in GDP

\widehat{PEg} = expected changes in the P/E ratio

\hat{Y} = the expected yield on the index

\widehat{RF} = the expected risk-free rate





Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

II. Macroeconomic Models (Supply-side estimates).

☐ Ibbotson-Chen (2003) model

- $\text{expected inflation} = (\text{YTM of 20-year T-bonds}) - (\text{YTM of 20-year TIPS})$
- $\text{growth in GDP} = \text{labor productivity growth rate} + \text{labor supply growth rate}$





Learning Outcome Statement 31

LOS 31.b: Calculate and interpret an equity risk premium using historical and forward-looking estimation approaches.

III. Survey estimates – use the consensus of the opinions from a sample of people.

- Strength: survey results are relatively easy to obtain
- Weakness: there may be a wide disparity between the consensuses obtained from different groups



Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

1. CAPM.
2. Multifactor Models

Required return=

$$\text{RF} + (\text{factor sensitivity})_1 * (\text{factor risk premium})_1 + \dots + (\text{factor sensitivity})_n * (\text{factor risk premium})_n$$





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

2.1 Fama-French model.

$$\text{required return of stock } j = RF + \beta_{\text{mkt},j} \times (R_{\text{mkt}} - RF) + \beta_{\text{SMB},j} \times (R_{\text{small}} - R_{\text{big}}) + \beta_{\text{HML},j} \times (R_{\text{HBM}} - R_{\text{LBM}})$$

The latter two of these factors corresponds to the return of a zero-net investment in the corresponding assets. The goal is to capture the effect of other underlying risk factors.



Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

2.1 Fama-French model.

E.g. Given the following market and stock data, calculate the required return on equity using the CAPM and the Fama-French models

$$(R_{\text{mkt}} - R_F) = 4.8\%$$

$$(R_{\text{small}} - R_{\text{big}}) = 2.4\%$$

$$(R_{\text{HBM}} - R_{\text{LBM}}) = 1.6\%$$

$$\text{risk-free rate} = 3.4\%$$

$$\beta_{\text{mkt},j} = 1.2$$

$$\beta_{\text{SMB},j} = 0.4$$

$$\beta_{\text{HML},j} = -0.2$$

CAPM: required return = $3.4 + 1.2 \times 4.8 = 9.16\%$

FF model: required return = $3.4 + 1.2 \times 4.8 + 0.4 \times 2.4 - 0.2 \times 1.6 = 9.48\%$





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

2.2 Pastor-Stambaugh Model

Add a liquidity factor to the Fama-French model.

Less liquid assets should have a positive beta, while more liquid assets should have a negative beta.





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

2.2 Pastor-Stambaugh Model

E.g. Assume a liquidity premium of 6% and the following factor risk premiums as well as sensitivities for the stock, calculate the cost of capital using the Pastor-Stambaugh model

$$(R_{\text{mkt}} - R_F) = 4.8\%$$

$$(R_{\text{small}} - R_{\text{big}}) = 2.4\%$$

$$(R_{\text{HBM}} - R_{\text{LBM}}) = 1.6\%$$

$$\text{risk-free rate} = 3.4\%$$

$$\beta_{\text{mkt},k} = 0.9$$

$$\beta_{\text{SMB},k} = -0.2$$

$$\beta_{\text{HML},k} = 0.2$$

$$\beta_{\text{liquidity},k} = -0.1$$

$$\text{Cost of capital} = 3.4 + 0.9 \cdot 4.8 - 0.2 \cdot 2.4 + 0.2 \cdot 1.6 - 0.1 \cdot 6 = 6.96\%$$





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

2.3 Macroeconomic Multifactor Model

❑ Burmeister, Roll and Ross model includes the following 5 factors:

1. Confidence risk
2. Time horizon risk
3. Inflation risk
4. Business cycle risk
5. Market timing risk





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

- ☐ Burmeister, Roll and Ross Model.
- ☐ E.g. use the following information to calculate the required return using a multifactor approach. The sensitivities for the stock is: 0.2, -0.2, 1.1, 0.3, 0.4, respectively and risk-free rate is 3%

| | | |
|---------------------|---|------|
| confidence risk | = | 2.0% |
| time horizon risk | = | 3.0% |
| inflation risk | = | 4.0% |
| business cycle risk | = | 1.6% |
| market timing risk | = | 3.4% |

$$\text{Required return} = 3 + 0.2 \times 2 - 0.2 \times 3 + 1.1 \times 4 + 0.3 \times 1.6 + 0.4 \times 3.4 = 9.04\%$$



Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

3. Build-up Method

Required return = RF + equity risk premium
+ size premium
+ specific-company premium

❑ Applicable to closely held companies.





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

3. Build-up Method

3.1 Bond-yield plus risk premium method.

- ☐ Add a risk premium to the YTM of the company's long-term debt
- ☐ Applicable to companies that have publicly traded debt.





Learning Outcome Statement 31

LOS 31.c: Estimate the required return on an equity investment using the capital asset pricing model, the Fama-French model, the Pastor-Stambaugh model, macroeconomic multifactor models, and the build-up method

3. Build-up Method

3.1 Bond-yield plus risk premium method.

E.g. Firm AA has bonds with 20-year 8% bond that is currently priced at 1100. An analyst estimates the equity risk premium for firm AA is 4%. Calculate the cost of equity using the bond-yield plus risk premium approach.

Answer: (1) 1000FV, 80PMT, 20N, -1100PV CPT I/Y=7.05%
(2) cost of equity = 7.05 + 4 = 11.05%



Thank You!

